

My office hours:

Today 1:30-2:45pm in MSC

Closing Tue:            Supp. 8-9

Closing Thu:            1.1, 1.2, 1.3

Midterm 1 is Tuesday, Oct 25

See Week 3 Newsletter online

*Entry Task:*

Let's start with a 10 min Q & A on the business terms. Do you have any questions on these topics?

*On the TC, VC graphs:*

Computing MC, AC, AVC?

Finding BEP and SDP?

Given a price, what do you do?

Maximizing profit?

Finding is FC?

*On the MC, AC, AVC graphs:*

Computing TC and VC?

Finding BEP and SDP?

Given a price, what do you do?

Maximizing profit?

## Section 1.1: Linear Equations (Skills)

*Motivation:* So far this entire course has been about **rates**. When we use a rate to predict the future, the equation we get is a line.

**Ex:** Husky football has average 49.5 points per game. In total they have scored 297 points so far this season. If this rate continues, how many total points will they have  $x$  games from now?

$$\text{Total points} = 297 + 49.5x$$

**Ex:** For electricity I pay a flat fee of \$30 per month plus \$0.05 per kilowatt hour of use.

$$\begin{aligned} \text{"payment for } x \text{ kilowatt hours of use"} \\ = 30 + 0.05x \end{aligned}$$

**Ex:** My savings earns 9% interest each year. Starting value =  $x$   
"interest from  $x$  (1 year)" =  $0.09x$   
"total value (1 year)" =  $x + 0.09x$

**Ex:** The ST stock starts at \$10 and increasing at a rate of \$5/month  
 $ST(x) = 10 + 5x = \text{'value in } x \text{ months'}$

**Ex:** Hats sell for \$5 per item.  
 $TR(x) = 5x$

We manufacture hats. Fixed costs equal \$200 each day and it costs \$3 to produce each hat.

$$TC(x) = 200 + 3x.$$

## Mathematical expressions:

a formula involving letters, numbers and operations; no equal sign

*Examples:*

$$\frac{5x}{2} - 3,$$
$$10 + \sqrt{3 + x},$$
$$5x - \frac{4}{x^{3/2}}$$

## Examples of linear equations:

$$3x + 4 = 10,$$
$$\frac{5x}{2} - 2 = 4x,$$
$$4(3 - 2x) = 16 + 5x$$

The goal will be to solve for  $x$ .

*Note:* All equations have equals signs **and** mathematical expressions on **both** sides.

## Examples of linear functions:

$$ST(x) = 10 + 5x$$

$$TR(x) = 5x$$

$$TC(x) = 200 + 3x$$

*Note:* All have a function name on the left! These are defining a rule. We are NOT solving these, these aren't equations. These are just giving a function a name.

**Linear functions** typically are written:

$$f(x) = mx + b \quad (\text{slope-intercept})$$

or

$$f(x) = m(x - x_0) + y_0 \quad (\text{point-slope})$$

## Fastest way to a linear function

Get two points on the line:

$$(x_0, y_0), (x_1, y_1)$$

*Step 1:* Find the slope:  $m = \frac{y_1 - y_0}{x_1 - x_0}$

*Step 2:* Write:  $y = m(x - x_0) + y_0$

**Example:** Find the equation of the line that goes through the points  
(2,10) and (4, 13)

- (a) Write in the point-slope form?
- (b) Write in slope-intercept form?
- (c) What is the y-intercept?
- (d) Sketch a graph of the line.
- (e) Is the point (5,16) on the line?

## **Skills Practice:**

Solving, Inequalities, etc..

## Some Application Problems:

*Example:* Cupcake Business

FC = \$300,

selling price = \$1.50/cupcake

production costs = \$0.50/cupcake

At what quantity will the profit be zero? (i.e. you will break even).

At what quantity will profit be \$450?

*Example:* You are told you have to average above 75% on the three exams to pass the class.

Assume you get 65% on your first test and 78% on your second test. What does your final exam score need to be in order to pass the class?

*Directly from homework:*

10) A retired woman has \$240,000 to invest. She has chosen one relatively safe investment fund that has an annual yield of 9% and another, riskier fund that has a 13% annual yield. How much should she invest in each fund if she would like to earn \$24,000 per year from her investments?